



Cambridge International AS & A Level

CANDIDATE
NAME

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MATHEMATICS

9709/21

Paper 2 Pure Mathematics 2

May/June 2024

1 hour 15 minutes

You must answer on the question paper.

You will need: List of formulae (MF19)

INSTRUCTIONS

- Answer **all** questions.
- Use a black or dark blue pen. You may use an HB pencil for any diagrams or graphs.
- Write your name, centre number and candidate number in the boxes at the top of the page.
- Write your answer to each question in the space provided.
- Do **not** use an erasable pen or correction fluid.
- Do **not** write on any bar codes.
- If additional space is needed, you should use the lined page at the end of this booklet; the question number or numbers must be clearly shown.
- You should use a calculator where appropriate.
- You must show all necessary working clearly; no marks will be given for unsupported answers from a calculator.
- Give non-exact numerical answers correct to 3 significant figures, or 1 decimal place for angles in degrees, unless a different level of accuracy is specified in the question.

INFORMATION

- The total mark for this paper is 50.
- The number of marks for each question or part question is shown in brackets [].

This document has **16** pages. Any blank pages are indicated.



- 1** A curve has equation $y = 2 \tan x - 5 \sin x$ for $0 \leq x < \frac{1}{2}\pi$.

Find the x-coordinate of the stationary point of the curve. Give your answer correct to 3 significant figures. [3]

[illegible]

2 A curve has equation $x^2 \ln y + y^2 + 4x = 9$.

Find the gradient of the curve at the point $(2, 1)$. [5]

[illegible]

- 3 (a) Sketch on the same diagram the graphs of $y = |3x - 8|$ and $y = 5 - x$. [2]

- (b) Solve the inequality $|3x - 8| < 5 - x$. [4]

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- (c) Hence determine the largest integer N satisfying the inequality $|3e^{0.1N} - 8| < 5 - e^{0.1N}$. [2]

4 (a) Show that $3 \tan 2\theta + \tan(\theta + 45^\circ) \equiv \frac{\tan^2 \theta + 8 \tan \theta + 1}{1 - \tan^2 \theta}$. [4]

This image shows a full page of white paper with horizontal dotted lines, typical of primary school writing paper. The lines are evenly spaced and run across the width of the page. There are no margins, text, or other markings on the paper.

(b) Hence solve the equation $3 \tan 2\theta + \tan(\theta + 45^\circ) = 4$ for $0^\circ < \theta < 180^\circ$. [3]

[illegible]

5 A curve has equation $y = \frac{1+e^{2x}}{1+3x}$. The curve has exactly one stationary point P .

(a) Find $\frac{dy}{dx}$ and hence show that the x -coordinate of P satisfies the equation $x = \frac{1}{6} + \frac{1}{2}e^{-2x}$. [4]

This image shows a full page of white paper with horizontal dotted lines, typical of primary school writing paper. The lines are evenly spaced and run across the width of the page. There are no margins, text, or other markings on the paper.

- (b) Show by calculation that the x -coordinate of P lies between 0.35 and 0.45 . [2]

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- (c) Use an iterative formula based on the equation in part (a) to find the x -coordinate of P correct to 3 significant figures. Give the result of each iteration to 5 significant figures. [3]

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- (b)** The shaded region is rotated completely about the x -axis.

Find the exact volume of the solid produced.

[6]

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- 7 The polynomial $p(x)$ is defined by

$$p(x) = 9x^3 + 6x^2 + 12x + k,$$

where k is a constant.

- (a) Find the quotient when $p(x)$ is divided by $(3x + 2)$ and show that the remainder is $(k - 8)$. [3]

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- (b) It is given that $\int_1^6 \frac{p(x)}{3x+2} dx = a + \ln 64$, where a is an integer.

Find the values of a and k . [6]

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[illegible]

Additional page

If you use the following page to complete the answer to any question, the question number must be clearly shown.

[illegible]

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